

Math exam

Linear algebra

Allons, courage et confiance !

1 Linear subspaces?

Everything must come with a justification.

1. Let $T \in \mathbb{R}^*$. We recall that a function $f : \mathbb{R} \rightarrow \mathbb{R}$ is T -periodic if $\forall x \in \mathbb{R}, f(x + T) = f(x)$. Is the set of T -periodic function a linear subspace of the linear space of function from \mathbb{R} to \mathbb{R} ?
2. Is $\{(x, y) \in \mathbb{R}^2 \mid x^2 + y^2 \leq 0\}$ a linear subspace of \mathbb{R}^2 ?
3. Is $\{(x, y, z) \in \mathbb{R}^3 \mid x + y = 0 \vee x + z = 0\}$ a linear subspace of \mathbb{R}^3 ?
4. Is the set of divergent sequences a linear subspace of the linear space of real-valued sequences?
5. Let $(a, b) \in \mathbb{R}^2$. Is the set of real-valued sequences $(u_i)_{i \in \mathbb{N}} \in \mathbb{R}^{\mathbb{N}}$ such that $\forall i \in \mathbb{N}, au_i + bu_{i+1} = u_{i+2}$ a linear subspace of the linear space of real-valued sequences?